## COUNT ON US

## SECONDARY CHALLENGE



## STUDENT WORKBOOK 2024

## GET ENGAGED IN MATHS!

## 1. INTRODUCTION

Welcome to your Count on Us Secondary Challenge student workbook.
This book contains two parts:
I. An introduction to tell you about the activities and the tournament, together with a tracker to help you find where the challenge activities fit with the maths topics you are learning in class.
2. Details about tournament activities, with rules and how it works in a tournament setting, together with activities for preparing for the tournament and to help you with your key stage 3 mathematics.

The Count on Us Secondary Challenge is a maths tournament involving over 4000 young people from across London, delivered by the Mayor's Fund for London in partnership with the Jack Petchey Foundation. We hope that by taking part, you will become more confident in maths, will develop your problem solving skills and boost your maths skills too.

The Secondary Challenge is made up of four rounds in different areas of maths. We hope you will find them really good fun and you'll want to practice lots to get really good at them! In the summer term, your school will select a team of 5 people to represent you in the regional heats.

This book will explain how all the activities work and give you everything you need to try them out, practice them and get really good at puzzling, problem solving and fast paced number skills. You will work on statistics and probability, geometry, algebra and different number skills, so everything that you do will help you with your ordinary maths lessons too.

The national curriculum in maths also expects you to develop three skills which are developed specifically in mathematics:
(i) Fluency: you can do maths quickly and accurately, mostly in your head (NO reaching for a calculator when you see simple numbers!)
(ii) Reasoning: you can see and describe how things work mathematically.
(iii) Problem Solving: you can find a mathematical way to solve problems.

The tournament has 4 rounds:

| I | Statistics and <br> Probability | This is in two parts (i) teams play the game of pig, a strategic dice <br> game needing thoughtful probabilistic thinking and (ii) Data-Chart- <br> Analysis, a card matching activity looking at statistical data, <br> illustrated with charts and analysed. |
| :--- | :--- | :--- |
| 2 | Geometry | You will play the game of GridLines Geometry, solving geometric <br> problems in different categories using randomly dealt number <br> cards. |
| 3 | Number | You will play the 24®Game. A card game requiring mental <br> number manipulation in a variety of categories: whole numbers, <br> integers and fractions and decimals. |
| 4 | Algebra | Your team will solve a series of algebra problems in a story based <br> context. |

Use the tracker starting on the next page to choose activities. The activities are coded as RI, R2, R3 or R4 (those used in the tournament, e.g. RI for round I, R2 for round 2 etc.

R2 activities are given more detail. The cards in the GridLines Geometry game are themselves coded by topic. $\mathrm{M}=$ Mensuration (Area and Perimeter), $\mathrm{V}=\mathrm{Volume}$ (and similarity), $P=$ Pythagoras and $A=$ Angles. So, if you see R2V look for the $V$ cards in the pack and so on.

The tracker covers all of the content of the Key Stage 3 National Curriculum. It has been simplified to include only those things you can work on independently.

## Tracker

| Number | R |
| :---: | :---: |
| 1. Place value for decimals, measures and integers of any size. |  |
| 2. Order positive and negative integers, decimals and fractions; on a number line and with symbols $=, \neq,<,>, \leq, \geq$ |  |
| 3. Prime numbers, factors (or divisors), multiples, common factors, common multiples, HCF, LCM and prime factorisation. |  |
| 4. Use the four operations with formal written methods. |  |
| 5. Use the four operations with integers (+ve and -ve numbers). | R3 |
| 6. Use the four operations with decimals. | R3 |
| 7. Use the four operations with fractions. | R3 |
| 8. Use priority of operations: brackets, powers, roots and reciprocals. | R3 |
| 9. Integer powers \& real roots (square, cube, 4, 5) as decimals and surds. | R3 |
| 10. Standard form $A \times 10^{n} 1 \leq A<10$, where n is +ve, -ve integer or 0 . |  |
| 11. Convert decimals and fractions and percentages | R3 |
| 12. Fraction Operations. |  |
| 13. Percentage; definition, calculation, comparison, change, operation. |  |
| 14. Round numbers and measures to appropriate degrees of accuracy. |  |
| 15. Round to estimate \& calculate possible resulting errors as $a<x \leq b$ |  |
| Algebra |  |
| 1. Algebraic notation: $a b, 3 y, a^{2}, a^{3}, a^{2} b, \frac{a}{b}$, coefficients, brackets. | R4 |
| 2. Substitute numerical values into formulae and expressions. | R4 |
| 3. Use vocab: expressions, equations, inequalities, terms and factors. | R4 |
| 4. Algebraic manipulations: collect like terms, multiply out brackets, take out common factors, expand products of binomials. | R4 |
| 5. Rearrange formulae to change the subject. |  |
| 6. Use algebraic methods to solve linear equations in one variable. | R4 |
| 7. Work with co-ordinates in all four quadrants. | R4 |
| 8. Graphs of linear and quadratic functions of one variable. | R4 |
| 9. Reduce linear equations to $y=m x+c$; gradients and intercepts. |  |
| 10. Use linear and quadratic graphs to estimate values and to find approximate solutions of simultaneous linear equations. |  |
| 11. Find approximate solutions to contextual problems from graphs, including piece-wise linear, exponential and reciprocal graphs. | R4 |
| 12. Terms of arithmetic, geometric and other sequences; nth terms with term-toterm or a position-to-term rules. | R4 |


| Ratio, proportion and rates of change |  |
| :---: | :---: |
| 1. Standard units e.g. time, length, area, volume/capacity, mass and compound units e.g. speed, unit pricing and density to solve problems. |  |
| 2. Use scale factors, scale diagrams and maps. |  |
| 3. Use ratio notation, including reduction to simplest form. |  |
| 4. Divide quantities as part:part or part:whole ratio; express as a ratio. |  |
| 5. Direct and inverse proportion; graphical and algebraic. |  |
| Geometry and measures |  |
| 1. Use perimeter, area and volume formulae for triangles, parallelograms, circles, trapezia, cuboids, other prisms. | R2M |
| 2. Ruler and compass constructions. |  |
| 3. Use conventional geometric terms and notations. | R2 |
| 4. Criteria for congruence of triangles and similarity by enlargement. | R2V |
| 5. Properties of triangles, quadrilaterals, circles, and other plane figures. |  |
| 6. Translations, rotations and reflections applied to given figures. |  |
| 7. Angles at a point, angles at a point on a straight line, vertically opposite angles, alternate and corresponding angles. | R2A |
| 8. Angle sum in any polygon, and properties of regular polygons. | R2A |
| 9. Use angle facts, similarity/congruence, Pythagoras' Theorem to obtain simple proofs. |  |
| 10. Use Pythagoras' Theorem and trigonometric ratios. | R2 |
| 11. Solve problems in 3-D using the properties of solid shapes. |  |
| Probability |  |
| 1. Record, describe and analyse probability experiments. | R1a |
| 2. Understand that the probabilities of all possible outcomes sum to 1 . |  |
| 3. Calculate theoretical probabilities using sample spaces. |  |
| Statistics |  |
| 1. One variable statistics: central tendency (mean, mode, median) and spread (range, consideration of outliers). | R1b |
| 2. Statistical tables, charts and diagrams: frequency tables, bar charts, pie charts, pictograms and vertical line (or bar) charts. | R1b |
| 3. Two variables statistics using scatter graphs. | R1 |

## 2. TOURNAMENT ACTIVITIES

Professional mathematicians explore mathematics having no idea what the outcome might be. This needs them to be prepared to carry on even when they have no idea at all. They never give up. You need to develop this skill!

The English mathematician Andrew Wiles describes what this feels like in a BBC Horizon programme 'Fermat's Last Theorem', which can easily be found with an internet search. Just watch the first two minutes and you'll be hooked.

The first round consists of two independent activities. The first is to play the Game of Hedgehog, which needs you to decide on strategy using probability. In the second you will match sets of cards showing data sets, statistic charts and analysis.

## ROUND Ia: The Game of Hedgehog

The Game of Hedgehog:
I. Two players or teams take turns.
2. In your turn: roll an ordinary die. If you roll $2,3,4$ or 5 then you score that amount. You can now choose to pass the turn to the other player or roll again. If you pass, you score the total you have made in this turn. If you roll again, you can add to your score if you roll $2,3,4$ or 5 . If you roll I then your turn over (but you can add the $I$ to your score for this round). If you roll a 6, then you score zero for this round and your turn is over.
3. The first player (or team) to reach 30 points is the winner.

Example game:

Player I rolls 5 then I turns ends turn score 6 Player 2 rolls 4 then 5 then 6 turn ends turn score 0 Player I rolls 4 then 3 then I turn ends turn score 8 Player 2 rolls 4 then 5 and passes turn score 9
Player I rolls 4 then 3 and passes turn ends turn score 7
Player 2 rolls 4 then 2 then 5 and passes turn score II
Player I rolls 5 then 3 and passes turn score 8
Player 2 rolls 3 then 5 then 3 and wins(!) turn score II

Player I: 6
Player I: 6 Player 2: 0
Player I: 14 Player 2: 0
Player I: 14 Player 2: 9
Player I: 19 Player 2: 9
Player I: 19 Player 2: 20
Player I: 27 Player 2: 20
Player I: 27 Player 2: 3I

In team play (and in the tournament) a team of 5 plays as one player, playing in turn within their team. They roll the dice in turn. They can either roll or pass. They must not communicate with each other in any way.

You should play this game many times. Try to decide on a strategy. When should you carry on rolling and when should you pass? Think about the level of risk and the reward. In the tournament, some points are awarded for winning the round, but most points are awarded for your score. So, even if you lose, you will score well if you have a high score like Player I in the example game.

Team play is much harder than individual play. So, we will use this version of the game in the tournament. When you have fully learned this version, for individual play you can move on to the 2 -dice game, which is a much better game for one v one.

## Two Dice Hedgehog:

I. Two players take turns.
2. In your turn: roll two ordinary die. If you roll $1,2,3,4$ or 5 on both dice then you score the total amount rolled. You can now choose to pass the turn to the other player or roll again. If you pass, you score the total you have made in this turn. If you roll again, you can add to your score if you again roll I, 2, 3, 4 or 5 on both dice. If you roll a 6 on either of the dice then you score zero for this round and your turn over. If you roll a double 6, then your total score zero is reset to zero and your turn is over.
3. The first player to reach 100 points is the winner.

Playing these games should help you get a sense for probability. You can find many more probability games here: https://nrich.maths.org/8494

## ROUND Ib: Data-Chart-Analysis

In this round, you will receive an envelope containing 18 mixed up cards. They will show 6 different situations. For each situation there is a set of data, a chart illustrating that data and some summary Analysis showing, for example, the average and spread of the data. Your job will be to find the 6 sets each with data, chart and analysis.

To prepare for this way of thinking, we suggest you try these activities from Nrich:

## Data

What's the Weather Like? https://nrich.maths.org/whatstheweatherlike
Chart
Olympic records
Statistics
About Average https://nrich.maths.org/l0995
In the tournament you will look at data from real world situations. In the news, in books on social media writers will make statements about information. They draw a conclusion (the Analysis) based on the data and often illustrate this with a chart. The relationship between these things is how statistics is used in practice.
You should search online for reports about things you are interested in, where charts and graphs have been used. Look at the relationship: Data-Chart-Analysis. This book from the European Union gives lots of examples to get you started: https://bit.ly/3EhgV8R.

Now try to match this sample set. Write an explanation to describe why you think the sets match. The answers are at the very end of this book. DO NOT look until you have thought hard to complete the matches!

## Data-Chart-Analysis Sample Card Set

| Data Card DI <br> Coastal tide gauges showing sea levels. | Chart <br> Card CI | Analysis <br> Card AI <br> "Renewable energy is getting cheaper." |
| :---: | :---: | :---: |
| Data Card D2 <br> The minimum amount of ice recorded in the Arctic each year. | Chart Card C2 | Analysis Card A2 <br> "The Paris Agreement could make a huge difference to world temperatures." |
| Data Card D3 <br> The amount of energyrelated carbon dioxide emissions across the world. |  | Analysis Card A3 <br> "Arctic ice caps are melting." |
| Data Card D4 <br> The cost of renewable energy in emerging-market economies. |  | Analysis Card A4 <br> "CO2 emissions are finally starting to level off." |
| Data Card D5 <br> The breakdown of carbon emissions by country. | Chart Card C5 | Analysis Card A5 <br> "Sea levels are rising." |
| Data Card D6 <br> Forecast data compiled by Climate Analytics, ECOFYS, and others. |  | Analysis <br> Card A6 <br> "China and the USA are responsible for the most carbon emissions." |

## ROUND 2: Gridlines Geometry

In this round you will play a card game, designed specially for this tournament called Gridlines Geometry. It has lots of geometric situations in; (i) angle relationships, (ii) using Pythagoras' theorem, (iii) finding perimeters and areas, (iv) finding volumes and lengths in similar figures.

In the game you must find particular solutions to general situations, using some of the ten number cards you will have been dealt.
For example, here is a situation:


You know that $x+y=180-75=105^{\circ}$
So, you would try to make for two numbers that fit. E.g. $50^{\circ}$ and $55^{\circ}$, or $20^{\circ}$ and $85^{\circ}$, or $37^{\circ}$ and $68^{\circ}$ etc. If you cannot find numbers to fit, there will always be two more problems to work on.

To prepare for this round, you should get lots of practice solving standard geometry problems in the three areas.
I. Practice your geometric problem solving.
a. www.bbc.com/bitesize/guides/zrck7ty/revision/I
b. www.bbc.com/bitesize/guides/z3g9q6/revision/I
c. www.bbc.com/bitesize/guides/z2mtyrd/revision/l
d. www.bbc.com/bitesize/guides/zc9wxnb/revision/l
2. Get confident using variables in geometry
a. Try this activity: $\underline{n r i c h . m a t h s . o r g / p e r i m e t e r e x p r e s s i o n s ~}$
b. Work through this: www.ocr.org.uk/Images/222109-topic-check-in-6.01-algebraic-expressions.pdf
c. Solve these: www.somerset.kI2.ky.us/userfiles/I03/Word\ Problems\ Perimeter\ a nd\%20Age.pdf
3. Take the level 0 cards in the Gridlines Geometry game pack (look for a 0 in the blue circle on the card). Work with a partner. Take turns to find a set of numbers that fits the situation. Find as many sets as you can. Now find level I cards and repeat. Now, level 2. These are quite hard! Finally, find level 3 cards and repeat. These are very hard - you would be best working together.
4. Now play a game of Gridlines Geometry. Read the rules on the next two pages, so you are clear about how it works.

## Gridlines Geometry Rules

Gridlines Geometry is a card game played with two 56 card decks consisting of:

- 6 Rules cards (to remind you of the rules in play).
- 3 'I give up’ cards (to use when you cannot find solutions to any problem).
- 44 Number cards.
- 9 Level 0 problems cards for getting started practice.
- 50 Geometric Problem cards.

The aim of the game is to find solutions to situations shown on Problem Cards, using numbers made from Number Cards. There are many possible solutions to each card. You must find numbers that can fit all the variables in the given situation.

## Playing the Game Summary

I. Take the 3 'I Give Up’ cards to use later.
2. Shuffle Number \& Problem Card packs and place them separately face down.
3. Place top 10 Number Cards in 2 rows of 5 face up $\& 3$ problem cards face up.
4. Solve Problem Cards using the Number Cards on the table. (Look at the Example Solution on the next page).
5. Take, keep and replace correctly solved Problem Cards. Return and replace used Number Cards.
6. Play an 'I Give Up' card at any time to replace any or all the number and/or Problem Cards.
7. Keep solving until the agreed time is up. Score I for each solved card.

## The Problem Cards



## The Number Cards

Number Cards can be organised into groups or played individually. Put the cards on top of one another to make a new number. When placed on the table, ONLY the required number can be visible.

## Examples



## Example Solution



I choose $\mathrm{a}=10$ and $\mathrm{b}=4$ because I can make 4 and 10 from the number cards.

- The area of the triangle AFD is $\frac{1}{2} \times 4 \times 10=20$
- The area of the square $A B C D$ is $10^{2}=100$
- So, the area of BCDF is $100-20=80$

If I can make 80 from the number cards, then I can show my solution.
(If not, choose different values for a and b and try again).
I show A, a, b using the number cards for $80,10,4$
You must use separate number cards for all the numbers.
A judge should check that the solution is correct.

## Notes

I. In competitive play, you must explain, step-by-step to the judge how your variables fit the situation. You can show important calculations you have made in your notebook if this helps.
2. When you play one 'I give up!' card you can swap as many cards as you like. All of the problem and number cards or some number and/or some problem cards. Replace the cards taken to return to ten number cards and three problem cards face up on the table. Now resume play.
3. Experienced players may wish to count the total number of points from the cards solved. (These are shown in the blue circle on each card as I, 2 or 3 , where 3 is the hardest).

## ROUND 3: The 24®Game. Whole Numbers, Fractions \& Decimals, Algebra \& Exponents

Ask an adult to do a calculation in their head and they'll run away! Everyone is scared of mental arithmetic. This round is designed to make sure YOU are not. All it needs is practice, practice, practice. (And a fun game to practice with ...)

The $24 ®$ Game is a card game. Each card has 4 numbers on it. You have to combine the numbers using,,$+- \times$ or $\div$ in any way you can to make an answer of 24 . You MUST use all four numbers once and once only!

See if you can do it with these numbers:
$\begin{array}{llll}4 & 5 & 8 & 4\end{array}$

Hints

- Try to find key number bonds: $6 \times 4,8 \times 3,16+8 \ldots$
- Try pairing the numbers up to make the parts you need.
- Try finding numbers to make I (to multiply and make no difference).
- Keep it all in your head!

Now try these:
I 526
236
$\begin{array}{llll}2 & 6 & 2\end{array}$
$\begin{array}{llll}1 & 5 & 3\end{array}$
2546

Don't forget ... we won't tell you the answers, so don't tell anyone else.
Use the next four pages to practice then use the 24®Game cards.

## Different 24®Game Cards

There are different types of $24 ®$ Game cards with different number types. You will have some cards of the different types to practice, they are:

- Single Digits: 4 single digit numbers.
- Double Digits: one or more of the numbers will be a two digit number.
- Fractions and Decimals: one or more of the numbers will be expressed as a fraction or a decimal.
- Integers: one or more of the numbers will be negative.
- Algebra and Indices:
- Algebra cards have one or more of the spaces replaced with an algebraic expression with variable $x$ and/or $y$. You choose any number(s) for the variable(s) (not zero) and use the value of the expression(s) to complete the 24.
- Indices cards have four index expressions (always $x^{2}, x^{3}, \sqrt{x}, \sqrt[3]{x}$ ). You choose one of these and apply one of the numbers on the card to make a new number, then use this and the others to complete the 24.

You should practice using each of the sets separately, then make sure you can still solve puzzles when the different types come up randomly. (Shuffle different types together to practice, but make sure to separate the packs to put them away!)

## TORTURE SQUARES

Practice your fractions calculations with these torture squares.
Complete each square using the operation shown:,,$+- \times$ or $\div$
Do them at different times.
Allow 10 minutes max to complete each square.

| + | 3 | $\frac{1}{2}$ |  | 4 | $\frac{3}{4}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\frac{1}{3}$ |  |  |  |  |  |
|  |  | $\frac{4}{5}$ |  |  |  |
|  |  |  |  |  | $1 \frac{1}{4}$ |
| $\frac{2}{3}$ |  |  |  |  |  |


| $\times$ | 8 | 0.1 | $\mathbf{2}$ | $\frac{1}{4}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\frac{1}{2}$ |  |  |  |  |  |
| 0.3 |  |  |  |  |  |
|  |  |  | 0 |  |  |
| 0.8 |  |  |  |  | 3.2 |
| $\frac{1}{3}$ |  |  |  |  |  |


| first number |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| - | $\mathbf{4}$ |  | $\frac{1}{4}$ | $\mathbf{7}$ | $\mathbf{0 . 3}$ |
| I |  |  |  |  |  |
| I.2 |  |  |  |  |  |
|  |  |  | $2 \frac{3}{4}$ |  |  |
| $\frac{1}{5}$ |  | 2.2 |  |  |  |
| $\mathbf{2}$ |  |  |  |  |  |


| first number |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\div$ | $\mathbf{6}$ |  |  | $\frac{2}{3}$ | $\mathbf{0 . 5}$ |
| $\mathbf{2}$ |  | $\mathbf{0}$ |  |  |  |
| $\mathbf{0 . 2}$ |  |  |  |  |  |
| $\frac{1}{4}$ |  |  | 4 |  |  |
| $\mathbf{5}$ |  |  |  |  |  |
| $\frac{1}{3}$ |  |  |  |  |  |

Make up more Torture Squares like these to test your friends.

## FIND 24: THE BOARD GAME

I. You will need sets of counters of two different colours; one for each player.
2. Take turns to find 24 using any four numbers on the board.

For example ( On board 1 on the next page): Use $4, \frac{1}{2}, 10,1.2$ make
$4 \times \frac{1}{2}=2$ and $10 \times 1.2=12$ then $2 \times 12=24$
Use a timer to give a maximum of one minute per turn.
3. If you succeed, place 4 counters on the number you found.
4. If you fail, your opponent takes a turn.
5. Numbers cannot be used more than once.
6. When neither player can make 24 in two consecutive rounds, play ends and the winner is the player who has placed the most counters.

## Alternative Rules:

I. Both players look for sets to make 24 at the same time.
2. If you find a set tap the table and play stops. Place your counters.
3. Score If all 4 numbers are whole numbers, add one for each fraction or decimal you used.
4. Play until both players agree they cannot find any more sets OR agree a time limit in advance.
5. For an even harder game, the set of four numbers must be next to each other on the board (horizontally, vertically or diagonally).

## Exponents Version:

You must substitute one of your numbers (but NOT the number 1) into one of the following expressions: $x^{2}, x^{3}, \sqrt{x}, \sqrt[3]{x}$

## Algebra Version:

You must substitute one or two of your numbers into one of these expressions before making 24 (when an expression has been used it cannot be used again):

| $x^{2}+1$ | $x(x+1)$ | $x^{2}+y$ | $\frac{x^{2}}{y}$ |
| :---: | :---: | :---: | :---: |
| $2 x(1-x)$ | $\frac{x^{2}}{y^{2}}$ | $x^{2}+2 y^{2}$ | $y\left(x^{2}-3\right)$ |
| $x\left(x^{2}+2 y\right)$ | $\frac{x+2 y}{x}$ | $x\left(3-y^{2}\right)$ | $\frac{3 x-y}{2 y}$ |

FIND 24 BOARD I (BEGINNER)

| 4 | $\frac{1}{4}$ | 6 | $\frac{1}{6}$ | 0.1 | 1 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 12 | $\frac{1}{8}$ | 3 | 9 | $\frac{1}{2}$ | 0.75 |
| 2 | 4 | 0.5 | 2 | 3 | 20 |
| 8 | $\frac{2}{3}$ | 1 | 3 | $\frac{1}{3}$ | 0.5 |
| $\frac{1}{4}$ | 9 | $\frac{3}{4}$ | 0.5 | 2 | 1 |
| 6 | $\frac{1}{2}$ | 4 | 10 | 0.25 | 6 |

FIND 24 BOARD 2 (INTERMEDIATE)

| 6 | $\frac{1}{4}$ | 3 | $I$ | $\frac{1}{3}$ | 8 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\frac{1}{4}$ | -2 | 0.5 | $\frac{1}{2}$ | 9 | $\frac{1}{2}$ |
| -12 | $\frac{1}{8}$ | 0.1 | 4 | 0.5 | 20 |
| 3 | 0.2 | $\frac{2}{3}$ | -3 | $\frac{1}{6}$ | 10 |
| $\frac{1}{12}$ | -9 | -4 | $\frac{5}{6}$ | 2 | $\frac{3}{4}$ |
| 1.5 | $\frac{2}{3}$ | 4 | 6 | 0.5 | -6 |

FIND 24 BOARD 3 (EXPERT)

| -7 | $\frac{1}{2}$ | 3 | 0.8 | $\frac{3}{5}$ | $I .5$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\frac{1}{3}$ | -2 | 0.5 | $\frac{1}{4}$ | -8 | $\frac{1}{12}$ |
| $2 \frac{1}{4}$ | $\frac{2}{3}$ | -1.2 | $1 \frac{1}{3}$ | 2.5 | $I I$ |
| 4 | -0.4 | $\frac{3}{8}$ | 2 | $\frac{1}{6}$ | $-1 \frac{3}{4}$ |
| $\frac{1}{2}$ | 9 | $I .3$ | $\frac{-2}{3}$ | 1.4 | $\frac{5}{12}$ |
| 0.3 | $\frac{5}{6}$ | -3 | $I \frac{1}{2}$ | 0.8 | 5 |

## ROUND 4: The Algebra Problem Solving Challenge.

Algebra is at the heart of all mathematics. It is the language that mathematicians use. You must speak it fluently! Also, you live in London, one of the world's greatest cities and you need to know it well. In this round, you need to use your fast-paced skill in algebra to decode messages to solve a problem about the city.
I. Read about your great city online to get an idea of the things that people think are important, but don't worry, all of the information you need will be given to you in the round.

- Go for a walk in London looking at maths: www.themathszone.com/? $\mathrm{p}=64 \mathrm{I}$
- Read about London at: en.wikipedia.org/wiki/London

2. You will need to practice your algebra. This list shows all the algebra problems you will need to know. Use it to decide what to practice.

- Algebraic notation: $a b, 3 y, a^{2}, a^{3}, a^{2} b, \frac{a}{b}$, coefficients, brackets.
- Substitute numerical values into formulae and expressions.
- Use vocabulary: expressions, equations, inequalities, terms and factors.
- Algebraic manipulations: collect like terms, multiply out brackets, take out common factors, expand products of binomials.
- Use algebraic methods to solve linear equations in one variable.
- Work with co-ordinates in all four quadrants.
- Graphs of linear and quadratic functions of one variable.
- Reduce linear equations to $y=m x+c$; gradients and intercepts.
- Terms of arithmetic, geometric and other sequences; nth terms with term-toterm or a position-to-term rules.

Practice algebra by making and solving Tarsia puzzles.

- First you will need to download the free Tarsia software at: www.mmlsoft.com/index.php/products/tarsia
- Then download the Algebra set of puzzles (scroll down to find them) at: www.mrbartonmaths.com/iigsaw.htm
- When the software is installed, choose one of the puzzles. Look at the examples on the algebra page (later in this booklet) to guide your choice. Open the file. Make sure the 'output' tab is selected. Print out the sheets. Cut them out. Put them together to make a large hexagon so that edges match with question and answer. ONLY when you have finished click the 'solution' tab.
- We recommend you work with a partner to solve these puzzles.


## Practice algebra by using GeoGebra.

- Go to https://www.geogebra.org/
- Click the START Calculator button. Try some things:
- Type: solve $(3 x+17=5 x+3)$ and press ENTER
- Type: simplify $(17 x+5 x-9 x)$
- Type: factor $\left(3 x^{\wedge} 2+6 x y\right)$
- Type: $y=3 x+1$ and press ENTER
- Type: $y=x^{\wedge} 2+3 x+1$ and press ENTER
- In GeoGebra always use $x, y$ and $z$ for your variables.
- Try different equations and expressions. Experiment. Explore!


## Data-Chart-Analysis Answers

| D6 | Cl | A2 |
| :---: | :---: | :---: |
| D4 | C2 | Al |
| D5 | C3 | A6 |
| DI | C4 | A5 |
| D3 | C5 | A4 |
| D2 | C6 | A3 |

Source with acknowledgement:
https://www.channel4.com/news/factcheck/climate-change-in-ten-graphs

